## MA 114 Worksheet #16: Review for Exam 02

1. List the first five terms of the sequence:

(a) 
$$a_n = \frac{(-1)^n n}{n! + 1}$$

(b) 
$$a_1 = 6$$
,  $a_{n+1} = \frac{a_n}{n}$ .

2. Determine whether the sequence converges or diverges. If it converges, find the limit.

(a) 
$$a_n = 3^n 7^{-n}$$

(c) 
$$a_n = \frac{\ln n}{\ln 2n}$$

(b) 
$$a_n = \frac{(-1)^{n+1}n}{n+\sqrt{n}}$$

$$(d) a_n = \frac{\cos^2(n)}{2^n}$$

3. Explain what it means to say that  $\sum_{n=1}^{\infty} a_n = 2$ .

4. Determine whether the geometric series is convergent or divergent. If it is convergent, find its sum.

(a) 
$$\sum_{n=1}^{\infty} \frac{(-4)^{n-1}}{3^n}$$

(b) 
$$\sum_{n=1}^{\infty} \frac{6 \cdot 2^{n-1}}{3^n}$$

5. Determine whether the given series converges or diverges and state which test you used.

(a) 
$$\sum_{n=2}^{\infty} \frac{1}{n \ln(n)}$$

(e) 
$$\sum_{n=1}^{\infty} \frac{9^n}{9n}$$

(b) 
$$\sum_{n=1}^{\infty} \frac{7\sqrt{n}}{5n^{3/2} + 3n - 2}$$

(f) 
$$\sum_{n=1}^{\infty} (-1)^{n+1} n e^{-n}$$

(c) 
$$\sum_{n=1}^{\infty} n! e^{-8n}$$

(g) 
$$\sum_{n=1}^{\infty} (-1)^{n-1} \arctan(n)$$

(d) 
$$\sum_{n=1}^{\infty} \left( \frac{\ln(n)}{5n+7} \right)^n$$

6. Determine whether each series is absolutely convergent, conditionally convergent, or divergent.

(a) 
$$\sum_{n=1}^{\infty} \frac{(-1)^n}{5n+1}$$

(c) 
$$\sum_{n=1}^{\infty} (-1)^n \cos\left(\frac{1}{n^2}\right)$$

(b) 
$$\sum_{n=1}^{\infty} \frac{(-1)^n}{n^3 + 1}$$

(d) 
$$\sum_{n=1}^{\infty} \frac{(n!)^n}{n^{4n}}$$

7. Find the radius and interval of convergence of each power series.

(a) 
$$\sum_{n=1}^{\infty} \frac{x^n}{4^n n^4}$$

(b) 
$$\sum_{n=1}^{\infty} \frac{(-1)^n x^n}{n^2}$$

(c) 
$$\sum_{n=1}^{\infty} \frac{(5x-4)^n}{n^3}$$

8. Find a power series representation for each function and determine its radius of convergence.

(a) 
$$f(x) = \frac{5}{1 - 4x^2}$$

(c) 
$$f(x) = \frac{3}{2+2x}$$

(b) 
$$f(x) = \frac{x^2}{x^4 + 16}$$

(d) 
$$f(x) = e^{-x^2}$$

9. Using the formula

$$\ln(1+x) = \int_0^x \frac{1}{1+t} \, dt$$

find a power series for ln(1+x) and state its radius of convergence.

10. Use the Maclaurin series for cos(x) to compute

$$\lim_{x \to 0} \frac{1 - \cos(x)}{x^2}.$$