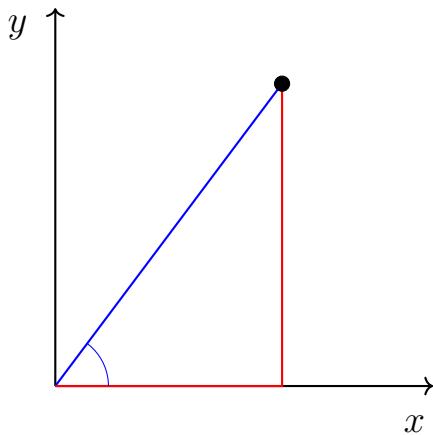


**Daily Announcements & Reminders:****Goals for Today:**

Sections 15.4, 15.5

- Introduce the polar coordinate system
- Convert double integrals to iterated polar integrals
- Compute iterated polar integrals
- Define triple integrals and compute basic triple integrals

**Polar Coordinates:**

**Cartesian coordinates:** Give the distances in \_\_\_\_\_ and \_\_\_\_\_ directions from \_\_\_\_\_

**Polar coordinates:**

- $r$  = distance from \_\_\_\_\_ to \_\_\_\_\_
- $\theta$  = angle between the ray \_\_\_\_\_ and the positive \_\_\_\_\_

We can use trigonometry to go back and forth.

**Polar to Cartesian:**

$$x = r \cos(\theta) \quad y = r \sin(\theta)$$

**Cartesian to Polar:**

$$r^2 = x^2 + y^2 \quad \tan(\theta) = \frac{y}{x}$$

**Example 83.** a) Find a set of polar coordinates for the point  $(x, y) = (1, 1)$ .

b) Graph the set of points  $(x, y)$  that satisfy the equation  $r = 2$  and the set of points that satisfy the equation  $\theta = \pi/4$  **in the  $xy$ -plane**.

c) Write the function  $f(x, y) = \sqrt{x^2 + y^2}$  in polar coordinates.

d) [Poll] Write a Cartesian equation describing the points that satisfy  $r = 2 \sin(\theta)$ .



## 15.4: Double Integrals in Polar Coordinates

**Goal:** Given a region  $R$  in the  $xy$ -plane described in polar coordinates and a function  $f(r, \theta)$  on  $R$ , compute  $\iint_R f(r, \theta) dA$ .

**Example 84.** Compute the area of the disk of radius 5 centered at  $(0, 0)$ .

**Remember:** In polar coordinates, the area form  $dA =$ \_\_\_\_\_

**Example 85.** Compute  $\iint_D e^{-(x^2+y^2)} dA$  on the washer-shaped region  $1 \leq x^2 + y^2 \leq 4$ .

**Example 86.** Compute the area of the smaller region bounded by the circle  $x^2 + (y - 1)^2 = 1$  and the line  $y = x$ .

**Example 87** (Poll). Write an integral for the volume under  $z = x$  on the region between the cardioid  $r = 1 + \cos(\theta)$  and the circle  $r = 1$ , where  $x \geq 0$ .

