

**MA114 Summer 2018**  
**Worksheet 25 – Calculus with Polar Curves – 7/26/18**

1. Find the slope  $dy/dx$  for the following polar curves:
  - a)  $r = 2 \cos(\theta) + 1$
  - b)  $r = \frac{1}{\theta}$
2. Compute the slope of the tangent line to the graph of  $r = \sin \theta$  at  $\theta = \pi/3$ , and sketch the curve and the tangent line.
3. Find the area enclosed by one leaf of the curve  $r = \sin 2\theta$ .
4. Find the arc length of one leaf of the curve  $r = \sin 2\theta$ .
5. Find the area between the inner and outer loop of the limaçon  $r = 2 \cos \theta - 1$ .
6. Find the tangent line to the polar curve  $r = \theta^2$  at  $\theta = \pi$ .
7. Find the length of the curve  $r = \theta^2$  for  $0 \leq \theta \leq 2\pi$ .
8. Find the area of the region that lies inside both the curves  $r = \sqrt{3} \sin \theta$  and  $r = \cos \theta$ .
9. Find the point(s) where the tangent line to the curve  $r = 2 + \sin \theta$  is horizontal.